Nighttime $D$-region electron density measurements from ELF-VLF tweek radio atmospherics recorded at low latitudes

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Abstract:

Dispersive atmospherics (tweeks) observed during 2010 simultaneously at two low latitude stations, Allahabad (geomagnetic lat., 16.79° N) and Nainital (geomagnetic lat. 20.48° N), have been utilized to estimate the nighttime D-region electron density at the ionospheric reflection height under the local nighttime propagation (21:00 – 02:00 LT or 15:30 - 20:30 UT). The analysis of simultaneously recorded tweeks at both the stations on five international quiet days during one month each from summer (June), winter (January) and equinox (March) seasons shows that the D-region electron density varies 21.5-24.5 cm$^{-3}$ over the ionospheric reflection height of 85-95 km. The average values of Wait lower ionospheric parameters: ionospheric reference height $h'$ and sharpness factor $\beta$ are almost same during winter (85.9 - 86.1km, 0.51-0.52 km$^{-1}$) and equinox (85.6-85.7 km, 0.54 km$^{-1}$) seasons. The values of $h'$ and $\beta$ during summer season are about 83.5 km and 0.60 km$^{-1}$ at both stations. Overall, equivalent electron density profile obtained using tweek method shows lower values of electron density by about 5-60% than those obtained using IRI-2007 model and lower/higher by 2-68% than those obtained using rocket technique. The electron density estimated using all three techniques (Tweek, IRI 2007, Rocket) is consistent in the altitude range of 82-98 km. The estimated geographic locations of causative lightnings of tweeks were matched with the locations and times of lightnings detected by the World-Wide Lightning Location Network (WWLLN). The WWLLN detected about 27.5% of causative lightnings of tweeks simultaneously observed at both the stations.
1. Introduction

The D-region of ionosphere ranges from ~ 60-75 km in the day and ~ 75-95 km in the night [Hargreaves, 1992]. It is the lowest part of Earth’s ionosphere where collisions between charged particles and neutrals dominate. It plays an important role in the propagation of Extremely Low Frequency (ELF: 30-3000Hz) and Very Low Frequency (VLF: 3-30 kHz) waves through the Earth-ionosphere wave-guide (EIWG) bounded below by the ground or the ocean and above by the D-region of the ionosphere. The D-region is too high for balloons and too low for the satellite measurements. The electron recombination and attachment rates in this region are so high that the free electron density is very small (<10^3 cm^-3) especially in the nighttime. Ground based radio sounding of the D-region particularly at the night by ionosonde, incoherent scatter and partial reflection radars do not work because of its low electron density [Hargreaves, 1992]. MF radars have been used [Igarashi et al., 2000] at some locations, but high cost of their operation is the main hindrance. For in-situ measurements of the lower ionosphere (up to ~ 150 km) rocket flights have been utilized [Maeda, 1971; Subbaraya et al., 1983; Gupta, 1998; Nagano and Okada, 2000; Friedrich and Torkar, 2001]. Rocket measurements of the D-region widely utilize either of two techniques; Faraday rotation [e.g., Friedrich and Torkar, 2001] and Langmuir probe [e.g., Subbaraya et al., 1983]. Friedrich and Torkar [2001] have given a historical review of the D-region rocket measurements globally. They have used about 118 rocket profiles to establish a model for non-auroral ionosphere. Their observations dealt with the rocket flights which were evenly distributed over the whole year, seasons, solar activity, day/night conditions covering up to 60° geomagnetic latitude. But limitation with the rocket technique is that it can be used only episodically and has limited spatial coverage, and cannot be used for continuous monitoring of the D-region. Thus the D-region remains the least studied
region of ionosphere. Since VLF waves are reflected by the D-region, fixed frequency VLF transmitter signals also have been successfully used to study the morphological features of the D-region [Thomson, 1993; Bainbridge and Inan, 2003; Thomson et al., 2007; Thomson and MacRae, 2009]. The disadvantage with VLF transmitter technique is its limited spatial coverage along the propagation path due to fixed number of VLF transmitters.

The ELF-VLF signals radiated by lightning discharges (global lightning flash rate ~ 50-100 sec\(^{-1}\) km\(^{-2}\)) [Rakov and Uman, 2006] can be used to investigate the D-region ionosphere globally. It is well known that lightning strikes radiate powerful radio bursts over a wide frequency range from few Hz to several MHz [Weidman and Krider, 1986] with a maximum spectral energy near 10 kHz [Uman, 1987; Ramachandran et al., 2007]. The radio bursts from the lightnings are called atmospherics or ‘sferics’ in short which propagate in the EIWG with low attenuation rate (2-3 dB/1000 km) [Yamashita, 1978; Davies, 1990]. The D-region has been studied using the VLF sferics [Cummer et al., 1998] and ELF sferics [Cummer and Inan, 2000] modeling using the Long Wave Propagation Capability (LWPC) Code developed by US Navy. They simulated for a variety of ionospheres, the VLF and ELF spectra of sferics received at 1000-2000 km away from the lightning sources. Using the same technique, Cheng et al. [2006] obtained the night-to-night variation of the D-region electron density over the East coast of the United States and compared it with the past nighttime rocket based data obtained at similar latitudes.

We have utilized the cutoff frequencies of different modes of dispersed sferics known as ‘tweeks’ to estimate the nighttime D-region electron density and Wait ionospheric parameters. Earlier studies on tweeks were mainly focused on the propagation properties of tweeks [Ohtsu, 1960; Yano et al., 1989 a & b; Yedemsky et al., 1992; Hayakawa et al., 1994, 1995; Sukhorukov,
1997; Ferencz, 2004; Ferencz et al., 2007; Kumar et al., 2008]. But in recent years the main focus has been to investigate the D-region ionosphere. Ohya et al. [2003] estimated equivalent nighttime electron density at the tweek reflection height at the low-middle latitudes by accurately reading the cutoff frequency of tweeks. They estimated equivalent electron density in the range of 20-28 cm\(^{-3}\) at the ionospheric reflection height of 80-85 km. Tweeks have also been used to estimate the ionospheric reflection height and their propagation distances along the propagation path [Kumar et al., 1994, 2008, 2009; Hayakawa et al., 1994; Maurya et al., 2010, 2012; Singh et al., 2011]. Kumar et al. [2009] developed a simple technique to calculate Wait ionospheric parameters; ionospheric reference height \( h' \) and exponential sharpness factor \( \beta \) from the cutoff frequencies of multimode tweeks observed at Suva, Fiji. The \( h' \) represents virtual reflection height in km and \( \beta \) represents the gradient in the D-region electron density in km\(^{-1}\).

In the present work we have utilized simultaneously recorded tweeks at the Indian low latitude stations, Allahabad and Nainital, during one year period January to December 2010, on five international quiet days during one month from summer (June), winter (January) and equinox (March) seasons, to study seasonal and day-to-day variability of the nighttime D-region reflection height and the electron density at the reflection height. We also present first results on nocturnal seasonal variation of \( h' \) and \( \beta \) using tweeks observed at these stations. The values of \( h' \) and \( \beta \) were obtained using tweek method developed by Kumar et al. [2009]. The previous studies on \( h' \) and \( \beta \) estimated using ELF-VLF sferics [Cummer et al., 1998; Cummer and Inan, 2000; Cheng et al., 2006; Han and Cummer, 2010a and b; Han et al., 2011] utilized data from few days to few months. In the present study we mainly focus on seasonal variation of \( h' \) and \( \beta \). The average values of \( h' \) and \( \beta \) have been used to obtain the electron density profile of the nighttime D-region up to 100 km altitude during three seasons (summer, winter and equinox).
Direction finding technique has been utilized to locate the source positions of tweeks (causative lightning discharges) to determine the path of propagation and hence the geographical area under investigation.

2. Summary of the Formulas Utilized

The EIWG is taken with perfectly reflecting walls separated by a distance $h$. The electromagnetic field in the waveguide can be comprised of a sequence of independent field structures (modes) that propagate with different group velocities. Each mode is defined by its cutoff frequency ($f_{cm}$). The $f_{cm}$ of $m^{th}$ mode is given [Budden, 1961] as

$$f_{cm} = \frac{mc}{2h} \quad (1)$$

Where $c$ is velocity of light in free space and $h$ is the tweek reflection height.

The electron density $n_e$ at the $h$ is estimated using the expression obtained by Shvets and Hayakawa [1998] and also utilized by Ohya et al. [2003] given as

$$n_e = 1.39 \times 10^{-2} f_{cm} \quad [\text{cm}^{-3}] \quad (2)$$

The group velocity $V_{gm}$ in the homogeneous spherical EIWG of $m^{th}$ mode is given [Ohya et al., 2008; Yano et al., 1989a] as

$$V_{gm} = c \left[ \left( 1 - \left( \frac{f_{cm}}{f} \right)^2 \right) \right]^{\frac{1}{2}} / \left( 1 - \frac{c}{2R f_{cm}} \right) \quad (3)$$

where $R$ is the radius of the Earth.

By calculating difference in arrival times, $\delta t = t_1 - t_2$ between two frequencies $f_1$ and $f_2$ close to $f_{cm}$ of tweeks, the $V_{gm}$ and hence the distance $d$ propagated by tweeks in the spherical EIWG can be calculated using

$$d = \delta t \left( \frac{V_{gf_1} \times V_{gf_2}}{V_{gf_1} - V_{gf_2}} \right) \quad (4)$$
where \( V_{gf1} \) and \( V_{gf2} \) are the group velocities of waves centred at the frequencies \( f_1 \) and \( f_2 \), respectively.

The distribution of charged particles in the ionosphere depends in a complicated way on latitude, solar zenith angle, season, and solar activity etc. In the simplest approach, the exponential increase of the lower-ionospheric electron density \( n_e \) expressed in \( \text{cm}^{-3} \), described by \textit{Wait profile} valid up to about 100 km altitude [\textit{Wait and Spies, 1964}] is obtained as

\[
n_e(h) = 1.43 \times 10^7 \exp(-0.15h') \exp[(\beta - 0.15)(h - h')] \tag{5}
\]

3. Data and Analysis

The ELF-VLF data recording system at both the sites, Allahabad and Nainital, consists of Stanford University designed Atmospheric Weather Electromagnetic System for Observation, Modelling and Education (AWESOME) VLF receiver [\textit{Cohen et al., 2010}]. Observational sites were established as a part of global AWESOME network under the auspices of the International Heliophysical Year [\textit{Scherrer et al., 2008; Singh et al., 2010}]. AWESOME system can record both broadband and narrow band data. Broadband data was recorded in the synoptic mode with 1 minute at every 15 minute interval. Narrowband data recording made in continuous mode gives the amplitude and phase of VLF transmitter signals which is not a part of present study. Broadband data is analysed using a Matlab code which produces dynamic spectrogram of selected durations showing atmospherics, tweeks and whistlers. The first order cutoff frequency \( f_c \) of tweeks in spectrograms was measured and used to calculate the ionospheric reflection height \( h \) and the D-region electron density \( n_e \) at the reflection height. The arrival times \((t_1 & t_2)\) of frequencies \((f_1 & f_2)\) were measured to determine propagation distance \( d \) of the tweeks. These frequencies and corresponding arrival times of tweek frequency components were measured with
frequency and time resolutions of 25.8 Hz and 1 ms, respectively, which correspond to an error of ~1.5 km in the reflection height for first mode and which reduces with the increase in the modes, ~0.40 cm$^{-3}$ in the electron density and ~500 km in the propagation distance. The error in electron density and propagation distance is same for all modes. We have utilized simultaneously recorded tweeks at Allahabad (geog. lat., 25.40º N; geog. long., 81.93º E; geomag. lat., 16.05º N) and Nainital (geog. lat., 29.35º N; geog. long., 79.45º E; geomag. lat., 20.48º N) on five international quiet days during one month from summer (June), winter (January) and equinox (March) seasons under the pure nighttime propagation (21:00–02:00 LT or 15:30 UT – 20:30 UT). A total of 1008 pair of tweeks (2016 tweeks) simultaneously observed were selected on the basis of clearly visible tweeks with intensity levels ≥ 60 dB as seen in the spectrograms. Tweeks observed within 2.0 ms interval at both the stations which corresponds to a distance of 600 km have been considered as simultaneously occurring tweeks as they were most likely originated from the same lightning source. The above selection criteria provided us with 400 pairs of tweeks during summer, 320 pairs during equinox and 288 pairs during winter. Out of 1008 pairs of tweeks, we have selected 990 pairs of tweeks with propagation distance ≤ 5000 km to avoid error in the reflection height and electron density due to tweeks coming from dayside propagation paths particularly for those tweeks which come from East-West directions. Finally, under this selection criterion we were left with 391 pairs during summer, 284 during winter and 315 during equinox.

There are three possible methods of calculating electron density from tweeks: (1) Using first order mode cutoff frequency of tweeks and equations 1 and 2. (2) Using the cutoff frequency of clear higher modes ($m \geq 1$) of tweeks and equations 1 and 2, and (3) Using the second method, we first calculate the electron density $n_e$ and the reflection height $h$ at least using
two modes of same tweek. The substitutions of $h$ and $n_e$ in equation 5 yield equations dealing with $h'$ and $\beta$ corresponding to the each value of $h$ and $n_e$ which on solving gives values of $h'$ and $\beta$ [Kumar et al., 2009]. Here, we have used above three methods and the results have been discussed and compared with rocket data and IRI 2007 model.

4. Results and Discussion

4.1 General Overview of Tweek Characteristics at Allahabad and Nainital

Broadband data recording at both the stations started in the year 2007 in the synoptic mode with 1 minute at every 15 minutes. Detailed analysis of tweek occurrence at Allahabad and Nainital shows that tweeks occur only in the local night between 18-06 LT [Maurya et al., 2012]. As an example, spectrograms containing typical multimode (up to 5th mode) tweeks observed simultaneously at both the sites on 16 March 2010 at 17 UT and on 14 June 2010 at 18:15 UT are shown in Figure 1 a & b. Local time (LT) = UT+5.5 hrs. The average tweek duration (dispersed section) is in the range of 8-48 ms at both the stations. The tweek duration of 10-50 ms remains same during winter and equinox seasons whereas during summer the tweek duration is comparatively less (5-35 ms). Seasonal variation in tweek duration indicates that during summer tweeks arrive from nearby lightning sources. It is due to the monsoon season (June – August) in India during summer when most lightning occur in the India, with more lightnings occurring around these stations, whereas during equinox and winter most of tweek lightning sources are located far in the Asia Oceanic Region. Kumar et al. [2008] reported the dispersion duration of 15-60 ms of the tweeks observed in the South Pacific Region. Reznikov et al. [1993] found tweek duration in the range of 40-50 ms, which may reach up to 100 ms. Thus tweek duration at our stations is comparatively less as compared with that reported by Reznikov et al.
[1993] and Kumar et al. [2008]. It is due to comparatively less propagation distance of tweeks to our stations as a good portion of the propagation path is over the land which offers more attenuation as compared to propagation over the ocean [Prasad, 1981]. Seasonal pattern of tweek occurrence shows a maximum during summer and almost same occurrence during winter and equinox at both the stations [Maurya et al., 2012]. During summer tweeks occur more frequently at Nainital than at Allahabad but during winter and equinox seasons tweek occurrence is more at Allahabad than at Nainital.

4.2 Night Time D-Region Reflection Height and Electron Density

The D-region of ionosphere acts as a good electrical conductor at the ELF and VLF frequencies. Lightning generated ELF-VLF tweeks form a useful diagnostic tool to estimate the nighttime ionospheric reflection height $h$ and the electron density $n_e$ at $h$. The $h$ at Allahabad and Nainital during three seasons (Summer, Winter, Equinox) determined from the cutoff frequency of first mode of tweeks and plotted in Figure 2 a & b shows nearly constant increase in the $h$ with time for all three seasons as indicated by the linear fit lines. The linear fit equations $y$ (km) = $mx + c$ are shown on the top of the Figures where $x$ is in hours. Table 1 shows maximum and minimum values of $h$ observed at both the stations during summer, winter and equinox seasons. The maximum and minimum values of $h$ are lower during equinox and winter as compared to those during summer. The $h$ also shows the day-to-day variability which is up to 9 km with a maximum variation of about 1-2 km on any day in any one hour duration (not shown here). It is also noted from linear fit equations shown in each panel of Figure 2 that temporal variability in the $h$ during selected period is higher during summer as compared to winter and equinox seasons with almost same variation during winter and equinox at both the stations.
By measuring the first mode cutoff frequency of tweeks and using equation (2) the $n_e$ at the $h$ has been calculated. Figure 3 shows variation in the nighttime $n_e$ at tweek $h$ during summer, winter and equinox seasons both at Allahabad and Nainital. It is noted that $n_e$ is higher by 2 cm$^{-3}$ during the summer as compared to that during winter and equinox seasons. The temporal variation of $n_e$ shows decrease in $n_e$ with time during three seasons. Average value of $n_e$ at Allahabad on selected days (15 day) varies 21–24.5 cm$^{-3}$ at the $h$ of 85-95 km and at Nainital 21.5-24 cm$^{-3}$ at the $h$ of 86-95 km. Using the same method, Ohya et al. [2003] estimated $n_e$ in the range from 20-28 cm$^{-3}$ at the $h$ of 80-85 km for a mid-latitude Japanese station.

The $h$ and $n_e$ variations with time can be understood mainly in terms of electron loss process and recombination in absence of major ionizing sources from sun. However, chemistry, ionization and recombination cycle of the D-region are complicated. The period of observation in present study falls under low solar activity period of solar cycle 23 with tweek propagation paths mainly over the low latitude and equatorial regions. Taking this into consideration we have tried to explain possible factors of the nighttime D-region variations shown in Figures 2 and 3. Ohya et al. [2011] reported that about 67% of nighttime lower ionospheric ionization is caused by Lyman-$\alpha$ and Lyman-$\beta$ coming from the geocorona which ionizes NO and O$_2$ at 95 km altitude. They have estimated electron densities at 95 km for NO$^+$ and O$_2^+$ which is about $5.5 \times 10^2$ cm$^{-3}$. Electron density at the reflection height estimated from first mode cutoff frequency of tweeks in the present work is less than $5.5 \times 10^2$ cm$^{-3}$ during three seasons. The less electron density in the nighttime can also be due to change in the neutral temperature in the recombination effect which is about a factor of ten [Ohya et al., 2011]. Another important source of ionization during nighttime is Galactic Cosmic Rays (GCRs) which has nearly half of ionization rate of Lyman-$\alpha$ at 85 km altitude [Thomson et al., 2007]. The GCRs intensity varies with solar activity with
maximum during solar minimum [Heaps, 1978]. The ionization by GCRs also depends on the geomagnetic latitude with minimum at the geomagnetic equator [Heaps, 1978]. Since period of study falls under solar minimum, GCRs are supposed to be the important ionizing source at the low and equatorial latitudes and hence an understating of GCRs variability during different seasons at the low and equatorial latitudes is essential to explain the D-region electron density variation.

The $h$ and $n_e$ at $h$ calculated for all modes of tweeks shown in Figure 1 using equations (1) and (2) are given in Table 2 (method 2). From the table 2, it can be noted that higher modes of any tweek are reflected comparatively from higher altitude (about 1-3 km for $m = 1$-5) with fundamental mode ($m = 1$) being reflected from lowest height. The results are consistent with the earlier findings of Shvets and Hayakawa [1998] and Kumar et al. [2008]. Theoretically, for a waveguide with perfectly conducting boundaries, the higher modes also should have been reflected from same altitude. Since the real EIWG is not perfectly conducting rather D-region forms a diffuse boundary of which conductivity/ionization increases exponentially with the altitude, the higher modes are reflected from slightly higher altitudes as compared to lower modes. Further the estimated values of mean cut-off frequency ($f_{cm}/m$) (as shown in Table 2) are slightly less for higher modes of tweek as compared to lower modes of same tweek. The electron density estimated from cutoff frequencies of first five modes of tweek shown in Figure 1a varies from 23-112 cm$^{-3}$ in the altitude range of about 1.7 km (89.9-91.5 km). The electron density for second mode is almost double to that obtained from first mode and so on for higher modes. The modes are reflected from the altitude where plasma frequency equals the cutoff frequency for that particular mode [Shvets and Hayakawa, 1998] which for higher modes happens where electron density (plasma frequency) and reflection height are higher. Since the electron density
of the D-region increases exponentially, the reflection height for higher modes increases accordingly. Shvets and Hayakawa [1998] from the cutoff frequency of modes \( m = 1-8 \) of tweeks observed during low solar activity months (January-April 1991) found an increase in the electron density from 28-224 cm\(^{-3}\) in the altitude range of about 2 km at an altitude of 88 km. Thus tweek method is useful in studying the variation in the electron density of the nighttime D-region ionosphere over a limited altitude range of about 1-2 km but requires clear multimode tweeks with at least three modes. The tweeks with higher modes (\( m > 3 \)) occur less frequently due to higher attenuation for the higher modes [Kumar et al., 2008; Maurya et al., 2012]. To overcome with height limitation of method 2 and less occurrence of tweeks with higher modes (\( m \geq 3 \)) tweeks, method 3, which gives \( h' \) and \( \beta \), has been utilized to estimate electron density and results are described in the section 4.3. Since frequency estimation of 25.8 kHz can lead the error up to \(~1.5\) km in the reflection height, the average values of \( h' \) and \( \beta \) for larger number (~300 in each season) of tweeks were used to minimize the error in estimation of variation of electron density with altitudes.

### 4.3. The \( h' \) and \( \beta \) Parameters Estimated from Tweeks

The lower ionosphere up to 100 km altitude [Wait and Spies, 1964] can be characterized by the reference height \( h' \) in km and the exponential sharpness factor \( \beta \) in km\(^{-1}\) as considered by many researchers [e.g. Cummer et al., 1998; Cummer and Inan, 2000; Thomson et al., 2007; Kumar et al., 2009; Han and Cummer, 2010a]. We have used the method developed by Kumar et al. [2009] to estimate the values of \( h' \) and \( \beta \) from first three modes of tweeks observed during summer, winter and equinox seasons. For this purpose we have selected 2 tweeks (total 10 from five quiet days) at every 15 minute interval (as recording was in synoptic mode with 1 minute at
each 15 minute interval) in the period of 21:00 - 02:00 LT on the five international quiet days of the months, January, March and June 2010. These months are taken as representative of winter, equinox and summer seasons. The method involves two steps; in first step the path integrated reflection height \( h \) and the electron density \( n_e \) are obtained using modes \( m = 1, 2, 3 \) of tweeks (mostly using \( m = 1-2 \)) by equation (1) and (2) for each selected tweek during three seasons. The values of \( n_e \) and \( h \) thus obtained have been used to calculate the values \( h' \) and \( \beta \) using equation (5) as described by Kumar et al. [2009]. The average values of \( h' \) and \( \beta \) on 5 quiet days thus obtained for Allahabad and Nainital during winter, summer and equinox are shown in Figure 4 & 5. The bars indicate the standard deviation. The estimated values of \( h' \) and \( \beta \) are nearly same at both the stations for the same season. However, there is a considerable day-to-day variability in \( h' \) and \( \beta \) of about 5 km and 0.2 \( \text{km}^{-1} \), respectively, which at any hour could be in the range of 4 km and 0.18 \( \text{km}^{-1} \). Seasonally, variability in \( h' \) is more during summer as compared to winter and equinox. The \( h' \) during summer at Allahabad varies 82.04 - 85.18 km with standard deviation (SD) ±1.58 to ±0.88 km and at Nainital it varies 82.08-84.30 km with SD ±1.17 to ±1.49 km. During winter \( h' \) varies 84.64-86.88 km with SD ±0.73 to ±0.54 km at Nainital and at Allahabad \( h' \) varies 85.36-86.88 km with SD ±0.93 to ±0.76 km. During equinox \( h' \) varies 84.9-86.77 km with SD ±0.37 to ±0.69 km at Allahabad and 84.86 - 86.30 km with SD ±0.82 to ±0.38 km at Nainital. The nighttime \( \beta \) during summer, winter and equinox varies between 0.53 - 0.67 \( \text{km}^{-1} \) with SD ±0.085 to ±0.078 \( \text{km}^{-1} \), 0.43 - 0.60 \( \text{km}^{-1} \) with SD ±0.002 to ±0.042 \( \text{km}^{-1} \) and 0.50 - 0.63 \( \text{km}^{-1} \) with SD ±0.074 to ±0.005 \( \text{km}^{-1} \) respectively, at Allahabad and between 0.54 - 0.68 \( \text{km}^{-1} \) with SD ±0.01 to ±0.057 \( \text{km}^{-1} \), 0.46 - 0.59 \( \text{km}^{-1} \) with SD ±0.08 to ±0.04 \( \text{km}^{-1} \) and 0.48 - 0.60 \( \text{km}^{-1} \) with SD ±0.063 \( \text{km}^{-1} \) to ±0.040 \( \text{km}^{-1} \) respectively, at Nainital. The variability is less during equinox and winter seasons at both the stations. The average estimated values of \( h' \) and \( \beta \) for
each season at both the stations are given in Table 3. Table 3 shows that $h'$ and $\beta$ are same at both stations. Seasonally, $h'$ and $\beta$ are same during winter and equinox but $h'$ is lower and $\beta$ is higher during summer.

There is only one previous study on $h'$ and $\beta$ parameters estimated using tweek method by Kumar et al. [2009]. Kumar et al. [2009] used tweek radio atmospheric observed at a low latitude in the South Pacific Region and found $h'$ and $\beta$ to be 83.1 km and 0.63 km$^{-1}$, respectively, during low solar activity period ($R_2 \sim 15$) between March to December 2006. Our values of $h'$ and $\beta$ shown in Table 3 match well with those of Kumar et al. [2009] during summer, but are higher during other two seasons. Cummer et al. [1998] using Long Wave Propagation Capability (LWPC) modeling of different ionospheres for VLF sferics observed during low solar activity month of July 1996 estimated nighttime values of $h'$ and $\beta$ 83.3 km and 0.49 km$^{-1}$, respectively. Our value of $\beta$ is higher up to 0.11 km$^{-1}$ than that obtained by Cummer et al. [1998]. Cheng et al. [2006] used similar procedure as used by Cummer et al. [1998] for sferics observed during 16 summer nights from 1 July to 4 August 2004 and obtained $h'$ and $\beta$ values in the range 83.6-85.6 km and 0.40-0.50 km$^{-1}$, respectively. Using sferics recorded during July-August 2005 in the nighttime, Han and Cummer [2010a] estimated hourly $h'$ between 82.0 km and 87.2 km with mean value of 84.9 km and standard deviation of 1.1 km. Our results on $h'$ are in good agreement with results reported by Han and Cummer [2010a]. Thomson et al. [2007] using LWPC modelling of phase and amplitude of VLF narrowband transmitter signals determined nighttime values of $h'$ = 85.1 ± 0.4 km and $\beta = 0.63 \pm 0.04$ km$^{-1}$ for the mid latitude D-region near solar minimum. Thomson and MacRae [2009] using LWPC modeling estimated $h'$ and $\beta$ to be 85.1 km and $\beta = 0.63$ km$^{-1}$, respectively, for equatorial and non-equatorial VLF
paths. The advantage of estimation of $h'$ and $\beta$ using tweeks over narrowband signal modelling is the larger geographic area covered around the observational site.

4.4. Equivalent Electron Density Profile and Comparison with IRI-2007 and Rocket Measurements

Tweek method utilized here gives path integrated electron density and reflection height. We have estimated average values of nighttime $h'$ and $\beta$, for summer, winter and equinox seasons. The values of $h'$ and $\beta$ estimated for each season are employed in equation (5) to calculate electron density profile in the altitude range of 80-100 km. Electron density calculated by tweek method has been compared with that obtained using IRI-2007 model and past Rocket measurements available in the Indian region.

4.4.1 Comparison with IRI-2007 Model

The IRI 2007 model gives electron density profile until year 2009 only. We have obtained electron density for the location of Allahabad and Nainital at 00:00 LT on five international quiet days during January, March and June of 2009. Since there is no difference in the solar activity level during 2009 and 2010, we take electron density during 2009 as the representative of 2010. IRI-2007 model shows no significant difference in the electron density profile for Allahabad and Nainital during summer, winter and equinox seasons and also no significant seasonal variation in the electron density profile at these stations. However, the values of $h'$ and $\beta$ obtained from tweek analysis and hence the electron density profile for summer is different than those for winter and equinox at both the stations. As shown in Figure 6 (panel a), during winter season electron density obtained from tweek method varies in the range of 4-6194 cm$^{-3}$ in the altitude range.
range of 80-100 km. Also the electron density thus obtained is quiet comparable to electron
density obtained from IRI-2007 in the altitude range of 91-95 km with a very good match at 94
km altitude but it is significantly low at the lower altitudes (Figure 6). The electron density
obtained from tweek method during summer season (Figure 6, panel b) varies in the range of 10-
95476 cm\(^{-3}\) in the altitude range of 80-100 km and shows a good comparison with IRI-2007 in
the altitude range of 82-89 km with very good match at 88 km. The electron density variation
during the equinox (Figure 6, panel c) is very much similar to that during winter with a very
good agreement in the altitude range of 89-93 km. In general, equivalent electron density profile
of the nighttime lower ionosphere using tweek method shows lower values of electron density by
about 5-60% than those obtained using IRI-2007 model at both the stations. Kumar et al. [2009]
have shown that electron density using tweek method is lower by about 20-45 % than those
obtained using IRI-2001 model at a low latitude station in the South Pacific Region. From the
analysis of tweek atmospherics observed in Japan, Ohya et al. [2003] found tweek estimated
electron density almost consistent with electron density profile obtained using IRI-95 model in
the altitude range of 80-85 km. The overall analysis shows that tweek method is useful for
estimating the electron density profile of the nighttime D-region ionosphere. Tweek method
shows seasonal variation in the nighttime D-region electron density whereas IRI 2007 model
does not show significant seasonal variation. The results are consistent with IRI-2007 model in
certain ranges of altitudes during different seasons.

4.4.2 Comparison with Rocket Data

Rocket data provides a direct measurement of electron density of the lower ionosphere.
Rocket experiment for the D-region electron density measurement at a low latitude, Thumba, an
Equatorial Rocket Launching Station (geographic lat., 8° 32´ N, magnetic dip., 0° 24´ S), in the Indian region, was carried out using Langmuir probe method on different types of rockets. The results of extensive series of measurements of lower ionospheric electron density at Thumba made under various solar and geographical conditions have been reported by Subbaraya et al.[1983]. We have selected nighttime rocket electron density data on 02 February 1968 at 18:56 Indian Standard Time (82.5º E) IST (sunspot number $R_z \sim 102$) and on 03 February 1973 at 00:30 IST ($R_z \sim 48$) for winter, on 29 August 1968 at 22:30 IST ($R_z \sim 105$) for summer and on 15 March 1975 at 22:04 IST ($R_z \sim 21$), on 12 March, 1967 at 22:30 IST ($R_z \sim 81$), on 21 April, 1975 at 23:00 IST ($R_z \sim 18$) for equinox season [Subbaraya et al., 1983]. During winter season, the trend of variation of electron density by tweek method is similar to rocket profile 1 in the altitude range of 86-98 km, and in the altitude range of 93-98 km for profile 2. The electron density is higher by about 30-52% in the altitude range of 86-94 km and lower by about 2-20% in the altitude range of 96-98 km with a good match in the range of 94-96 km. Similarly electron density is lower by about 3-40% in the altitude range of 96-98 km with good match at 95 km as compared to rocket profile 2. During summer season, the electron density measured by rockets varies consistently with the electron density estimated by tweek method in the altitude range of 87-93 km with a difference of about 15-58%. For equinox season, electron density is available for three rocket profiles only which vary concurrently with electron density profile estimated by tweek method in the altitude range of 89-94 km, 92-94 km, 92-95 km but with lower/higher values by 32-68%, 2-55% and 6-65%, respectively. The difference in the electron density is due to the fact that some of the rocket experiments were conducted during high solar activity period. Overall the trend of variation of electron density calculated by tweek method is consistent with available rocket electron density profiles in the altitude range of 86-98 km with a difference in
electron density of about 2-68% during different seasons. Seasonal variation in the electron density estimated by tweek method is consistent with the seasonal variation observed with the rocket experiments [Gupta, 1998]. The electron density estimated by all three techniques is consistent in the altitude range of 82-98 km indicating that tweek method is also useful for obtaining electron density profile of the nighttime D-region.

Thomson et al. [2007] estimated the nighttime electron density of about 40 cm$^{-3}$ generated by Lyman-$\alpha$ of geocorona at the altitude of 85 km which is higher compared to our tweek measurements (27 cm$^{-3}$ during winter and 28 cm$^{-3}$ during equinox) as shown in Figure 6. The main sources of day-to-day and temporal variability of the nighttime D-region electron density and $h'$ and $\beta$ have been explained in section 4.2. The variations can also be due to the presence of metal ions ($\text{Fe}^+$, $\text{Mg}^+$), probably of meteor origin, which are left out from the daytime ionization, because of slow recombination rate. The electron density due to metal ions has been reported $\sim$10$^3$ cm$^{-3}$ at 90 km altitude [Akin and Goldberg, 1973; Kopp, 1997]. This at least partially explains the higher electron density of 1000 cm$^{-3}$ estimated during summer at 90 km as compared to the electron density during winter and equinox seasons at the same altitude which is 170 cm$^{-3}$ and 200 cm$^{-3}$, respectively. Other factor which can contribute to variation in the nighttime electron density at different altitudes is possibly the formation of water cluster ions below 85 km [Reid, 1997]. The electrons recombine very rapidly with these cluster ions and electron density falls rapidly with decreasing height. Thomson and MacRae [2009] suggested that irregularities in the equatorial electrojet may be associated with gradient drift instabilities) can penetrate nighttime D-region ionosphere down up to 90 km altitude and cause the scattering of VLF waves on passing over equator and can contribute to the variability in $h'$ and $\beta$. Lower ionospheric temperature variation caused by the presence of atmospheric waves [Sugiyama, 1988] can also
cause the variation in the electron density however, there is no direct observation of atmospheric waves in our tweek data.

4.5. Estimation of Locations of Causative Lightning Sources of Tweeks

Since tweek method gives the path integrated reflection height and electron density at the reflection height, it is also important to find the locations of tweek causative lightnings and hence the propagations paths over which the reflection height and the electron densities are obtained. There are two techniques widely used for lightning detection; multi station technique [Ohya et al., 2003] and single station technique [Ramchandran et al., 2007]. We have used multi station technique (two station) developed by Ohya et al. [2003] for simultaneously recorded 1008 pairs (2016 total) clear and long duration tweeks at Allahabad and Nainital during one year period from January to December 2010, in the pure nighttime (21:00-02:00 LT, or 15:30 – 20:30 UT), to locate the causative lightnings of tweeks. The propagation distances $d$ of these simultaneously recorded tweeks to both the stations were calculated using equation (4) and circles of those radii with centre at the location of stations were drawn. The location of causative lightning of any tweek was determined by the intersection of two circles corresponding to the propagation distance of same tweek to Allahabad and Nainital. The locations of intersection points were matched with the World-Wide Lightning Location Network (WWLLN) lightning data. The WWLLN is the worldwide lightning location network in which 40 universities and research institutions are currently participating worldwide. It detects global lightnings with return stroke currents $> 50$ kA with spatial and temporal accuracy of about 10 km and 10 μs, respectively, with global detection efficiency less than 4% [Rodger et al., 2006]. However, with the increase in the number of stations its detection efficiency has improved up to 10%. The WWLLN
detected the causative lightings for 277 (27.5%) tweeks out of total 1008 tweeks as shown by the overlap of red circles (WWLLN detected lightnings) over green circles (locations estimated using two station tweek observation method). From Figure 7 we can see that causative lightning sources of tweeks were located in the wide range but majority of them (~65%) were in the South East Asian region (20 -10° N, 75-130° E). Figure 7 also gives the comparison of lightning source positions calculated by tweek method (green circle) with those detected by the WWLLN (red circles) for winter, summer and equinox, respectively. In Figure 7 we have also drawn three circle of radius 1000 km, 3000 km and 5000 km to show the causative source lightning distances with respect to the receiving site Allahabad. Most of the tweeks propagated more than 1000 km and about 60% tweeks propagated in the range of 3000-5000 km.

The direction finding technique applied here shows that most tweeks observed in the Indian sector come from south East Asian region, which is one of the most lighting activity regions of the world [Christian et al., 2003]. The day-to-day variability in $h'$ and $\beta$ estimated from tweeks shown in Figure 4 & 5 can also be caused by heating of the D-region by lighting discharges. Han and Cummer [2010a] found a good correlation between $h'$ and the rate of lightning strokes. They have concluded that either direct lightning coupling to the ionosphere or ducted lightning-induced electron precipitation can drive significant D-region variability on the time scales from minutes to hours. At our stations direct lightning coupling to the ionosphere producing short-term (10-100 s) significant electron density changes is most likely the source of day-to-day variability as lightning-induced electron precipitation is very unlikely to occur in the low-latitude region [Voss et al., 1998]. The direct energy coupling between lightning discharges and lower ionosphere causing short-term changes in the electron density or conductivity at the VLF reflection heights have been reported by many researchers [e.g. Inan et al., 1988; Rodger,
2003 and references therein]. The heating of lower ionosphere by strong quasi-electrostatic field
generated by strong lightnings causes the conductivity enhancements [e. g. Pasko et al., 1995; 
Inan et al., 1996; Inan et al., 2010] and the electromagnetic pulses from cloud-to-ground and/or
successive in-cloud lightning discharges associated with cloud-to-ground discharges can produce
appreciable electron density changes which could be the electron density
enhancements/reductions at the VLF reflection height [Inan et al., 1993; Rodger et al., 2001; 
Marshall et al., 2008].

5. Summary and Conclusions

The dispersed sferics called tweeks observed using Stanford University designed
AWESOME VLF receiver system installed at Allahabad and Nainital during one year period
January to December 2010 were analyzed for the pure nighttime 21:00-02:00 LT (21:00-02:00
LT) propagation. The simultaneously observed tweeks at both the stations were used to estimate
the path integrated tweek reflection heights and electron densities at the reflection heights. For
the first time nocturnal and seasonal variations of the nighttime Wait ionospheric parameters ($h'$
and $\beta$) have been studied by using tweeks observed at the low latitude stations Allahabad and
Nainital, in the Indian region. The average values of $h'$ and $\beta$ for seasons summer, winter and
equinox have been estimated to obtain the seasonal electron density profile of the D-region and
compared with IRI 2007 model and earlier rocket measurements in India. The main findings of
the study can be concluded as

1. The path integrated reflection height $h$ of nighttime D-region ionosphere calculated by using
   first order cutoff frequency of tweeks varies in the range 87-95 km at both the stations. The
path integrated electron density $n_e$ estimated using first order cutoff frequency of tweeks varies as 21-24.5 cm$^{-3}$ at Allahabad and 21.5-24 cm$^{-3}$ at Nainital.

2. The nocturnal and seasonal variability in the $h'$ and $\beta$ at both the stations shows that the nighttime D-region is far from static. The average values of $h'$ and $\beta$ for both the stations are almost same (86.1-85.6 km, and 0.51-0.54 km$^{-1}$) during winter and equinox seasons. The $h'$ is lower by 2-3 km and $\beta$ is higher by 0.07-0.09 km$^{-1}$ during summer as compared to winter and equinox seasons.

3. The day-to-day variability in $h$ is about 8-9 km with temporal variability of 1-2 km in any one hour duration. The day-to-day variability in $h'$ is about 4-5 km and in $\beta$ it is about 0.1-0.25 km$^{-1}$. The $n_e$ obtained using tweek method shows lower values than those obtained using IRI-2007 model and higher during winter and equinox and lower during summer when compared with Rocket data, however, the trend of $n_e$ variation in the altitude range of 85-98 km is almost the same. This shows that tweek method is one of the useful methods for estimating the electron density profile of the nighttime D-region ionosphere.

4. The $n_e$ obtained using tweek method shows seasonal variation with higher values during summer as compared to winter and equinox seasons but IRI-2007 model does not show any seasonal variation.

5. The locations of causative lightnings obtained using tweek method and compared with WWLLN detected lightings show that the lightning sources of most tweek were located in the Asia Oceanic region. The WWLLN detected about 27.5% of lightnings associated with tweeks.

Acknowledgements
Authors from Indian Institute of Geomagnetism (IIG) are grateful to Director, IIG for support and encouragement to carry out the project and work. All authors thank International Space Weather Initiative Program (ISWI) and United Nations Basic Space Sciences Initiative (UNBSSI) program for their support. Thanks to CAWSES India, Phase-II program for the financial support in form of project to carry out VLF research activities at IIG.

Robert Lysak thanks the reviewers for their assistance in evaluating this paper.

References


Kumar, S., A. Deo, and V. Ramachandran (2009), Nighttime D-region equivalent electron density determined from tweek sferics observed in the South Pacific Region, *Earth Planets Space*, 61, 905-911.


**Table 1:** Seasonal maximum and minimum values of the reflection height at Allahabad and Nainital during 2010.

<table>
<thead>
<tr>
<th>Seasons</th>
<th>Allahabad Tweek reflection (km)</th>
<th>Nainital Tweek reflection (km)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Minimum</td>
<td>Maximum</td>
</tr>
<tr>
<td>Summer</td>
<td>84</td>
<td>96</td>
</tr>
<tr>
<td>Winter</td>
<td>87</td>
<td>95</td>
</tr>
<tr>
<td>Equinox</td>
<td>87</td>
<td>95</td>
</tr>
</tbody>
</table>
**Table 2**: The mode number, cutoff frequency, mean cutoff frequency, ionospheric reflection height $h$, and electron density $n_e$ for tweeks shown in the spectrogram for modes $m=1$-5.

<table>
<thead>
<tr>
<th>Station</th>
<th>Mode</th>
<th>Cutoff frequency</th>
<th>Mean Cutoff frequency</th>
<th>Reflection height</th>
<th>Electron density</th>
</tr>
</thead>
<tbody>
<tr>
<td>Allahabad</td>
<td>(a)</td>
<td>1.6693 kHz</td>
<td>1.6693 kHz</td>
<td>89.9 km</td>
<td>23.20 cm$^{-3}$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>3.3212 kHz</td>
<td>1.6606 kHz</td>
<td>90.3 km</td>
<td>46.16 cm$^{-3}$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>4.9546 kHz</td>
<td>1.6515 kHz</td>
<td>90.8 km</td>
<td>68.87 cm$^{-3}$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>6.5839 kHz</td>
<td>1.6460 kHz</td>
<td>91.0 km</td>
<td>91.52 cm$^{-3}$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>8.1933 kHz</td>
<td>1.6387 kHz</td>
<td>91.5 km</td>
<td>113.89 cm$^{-3}$</td>
</tr>
<tr>
<td>(b)</td>
<td>1.6159 kHz</td>
<td>1.6159 kHz</td>
<td>92.8 km</td>
<td>22.46 cm$^{-3}$</td>
<td></td>
</tr>
<tr>
<td></td>
<td>3.1918 kHz</td>
<td>1.5959 kHz</td>
<td>94.0 km</td>
<td>44.37 cm$^{-3}$</td>
<td></td>
</tr>
<tr>
<td></td>
<td>4.7843 kHz</td>
<td>1.5948 kHz</td>
<td>94.1 km</td>
<td>66.50 cm$^{-3}$</td>
<td></td>
</tr>
<tr>
<td></td>
<td>6.3168 kHz</td>
<td>1.5792 kHz</td>
<td>95.0 km</td>
<td>87.80 cm$^{-3}$</td>
<td></td>
</tr>
<tr>
<td>Nainital</td>
<td>(c)</td>
<td>1.6693 kHz</td>
<td>1.6693 kHz</td>
<td>89.9 km</td>
<td>23.20 cm$^{-3}$</td>
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<tr>
<td></td>
<td></td>
<td>3.2986 kHz</td>
<td>1.6493 kHz</td>
<td>90.9 km</td>
<td>45.85 cm$^{-3}$</td>
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<tr>
<td></td>
<td></td>
<td>4.9813 kHz</td>
<td>1.6604 kHz</td>
<td>90.3 km</td>
<td>69.24 cm$^{-3}$</td>
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<tr>
<td></td>
<td></td>
<td>6.6374 kHz</td>
<td>1.6593 kHz</td>
<td>90.4 km</td>
<td>92.26 cm$^{-3}$</td>
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<tr>
<td>(d)</td>
<td>1.6159 kHz</td>
<td>1.6159 kHz</td>
<td>92.8 km</td>
<td>22.46 cm$^{-3}$</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>3.1651 kHz</td>
<td>1.5825 kHz</td>
<td>94.8 km</td>
<td>44.00 cm$^{-3}$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>4.7943 kHz</td>
<td>1.5981 kHz</td>
<td>93.9 km</td>
<td>66.64 cm$^{-3}$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>6.3128 kHz</td>
<td>1.5782 kHz</td>
<td>95.1 km</td>
<td>87.75 cm$^{-3}$</td>
</tr>
</tbody>
</table>

**Table 3**: Seasonal average values of reference height $h'$ and sharpness factor $\beta$ for Allahabad and Nainital during 2010.
<table>
<thead>
<tr>
<th>Seasons</th>
<th>Allahabad</th>
<th>Nainital</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$h'$ (km)</td>
<td>$\beta$ (km$^{-1}$)</td>
</tr>
<tr>
<td>Summer</td>
<td>83.54</td>
<td>0.61</td>
</tr>
<tr>
<td>Winter</td>
<td>85.87</td>
<td>0.51</td>
</tr>
<tr>
<td>Equinox</td>
<td>85.74</td>
<td>0.54</td>
</tr>
</tbody>
</table>

**Figure 1**: Spectrograms showing typical twicks observed simultaneously at Allahabad and Nainital.

**Figure 2**: Variation in the reflection height estimated from first mode cutoff frequency of 990 twicks simultaneously recorded at Allahabad and Nainital in pure night time 21:00-02 LT (15:30-20:30 UT) conditions. The trend of variation in the reflection height is shown by the linear fit lines and equations.

**Figure 3**: Variation in the electron density estimated from first mode cutoff frequency of 990 twicks simultaneously recorded at Allahabad and Nainital in pure night time 21:00-02 LT (15:30-20:30 UT) propagation. The trend of variation in the electron density is shown by the linear fit lines and equations.

**Figure 4**: Variations of the nighttime ionospheric D-region parameters; reference height $h'$ and sharpness factor $\beta$ during three seasons, summer, winter and equinox at Allahabad.

**Figure 5**: Variations of the nighttime ionospheric D-region parameters, reference height $h'$ and sharpness factor $\beta$ during three seasons, summer, equinox and winter at Nainital.
Figure 6: A comparison of electron density profiles of the D-region obtained using tweek method, IRI-2007 Model, and rocket data during winter, summer and equinox seasons. Error bars shown in IRI-2007 data are standard deviations.

Figure 7: Locations of tweek causative lightning discharges determined by tweek method (green color) simultaneously at Allahabad and Nainital during winter, summer and equinox seasons of 2010. The WWLLN detected lightning locations are indicated in red color.